

Definition: $\cup A = \{x : \exists y x \in y \in A\}$.

Exercises.

$$\cup \{[0, 1/n] : n = 1, 2, 3, \dots\} = [0, 1]$$

$$\cup \{[0, n] : n \in \mathbb{N}\} = \mathbb{R}^{\geq 0}$$

$$\cup \{(1/n, 1) : n = 1, 2, 3, \dots\} = (0, 1)$$

$$\cup \{[1/n, 1] : n = 1, 2, 3, \dots\} = (0, 1)$$

$$\cup \{[n, 2n] : n = 1, 2, 3, \dots\} = \{0\} \cup [1, \infty)$$

$$\cup \{p\mathbb{Z} : p \text{ prime}\} = \mathbb{Z} \setminus \{-1, 1\}$$

$$\cup \{[1/n, 1 - 1/n] : n = 1, 2, 3, \dots\} = (0, 1)$$

$$\cup \{(\infty, 1 - 1/n] \cup [1 + 1/n, \infty) : n = 1, 2, 3, \dots\} = \mathbb{R} \setminus \{1\}$$

$$\cup \{[n, n^2] : n = 1, 2, 3, \dots\} = [2, \infty) \cup \{0, 1\}$$

$$\cup \{[n, n^3] : n \in \mathbb{Z}\} = [2, \infty) \cup \{-1, 0, 1\}$$

$$\cup \{p\mathbb{Z} : p \text{ odd prime}\} = \mathbb{Z} \setminus \{\pm 2^n : n \in \mathbb{N}\}$$

$$\cap \{p\mathbb{Z} : p \text{ prime}\} = \{0\}$$

$$\cap \{[n - 1/n, 1 + 1/n] : n = 1, 2, 3, \dots\} = \{1\}$$

$$\cap \{(1 - 1/n, 1 + 1/n) : n = 1, 2, 3, \dots\} = \{1\}$$

$$\cap \{(1 - 1/n, 2 + 1/n) : n = 1, 2, 3, \dots\} = [1, 2]$$

$$\cap \{[n, \infty) : n = 1, 2, 3, \dots\} = \emptyset$$